

Name: _____

Partner(s): _____

Date: _____

Physical Optics (considering *phase shifts*)

Background

An interesting optical effect stands out when light encounters a small aperture or barrier, such as a pinhole or a fine slit or single strand of hair. This effect is known as diffraction and is a consequence of the fact that light propagates like a wave (and ***not*** in the way suggested by the simple ray diagrams used in the geometric optics approximation): in particular, we will see that **phase shifts** (whether due to differences in path length or in the media traversed) can have enormous consequences on the transmitted beam shape.

Procedure

The experimental setup is shown in Figure 1. A monochromatic Helium-Neon laser, having a known wavelength of $\lambda = 632.8 \text{ nm}$, is positioned on the short bench. The laser should be positioned such that it points to the center of the screen. Objects causing diffraction will be positioned just a few centimeters from the laser. To get the greatest resolution, the (measured) **distance between the object and the observing screen, L , should be as large as possible.**

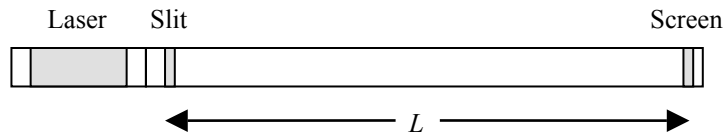


Figure 1

Part 1: Circular Apertures

Each station has been supplied with *two* small circular apertures. At most stations, these are *both* located on Slide 9165-D. (Masking tape has been used to cover, temporarily, parts of the slide that are not in use for this part of your lab work; please leave that in place.) In any case, your first step is to introduce the **larger** of these two small circular apertures into the beam path, and to record your estimate of the **size** of the resulting spot on your imaging screen.

Aperture diameter = _____

L = _____

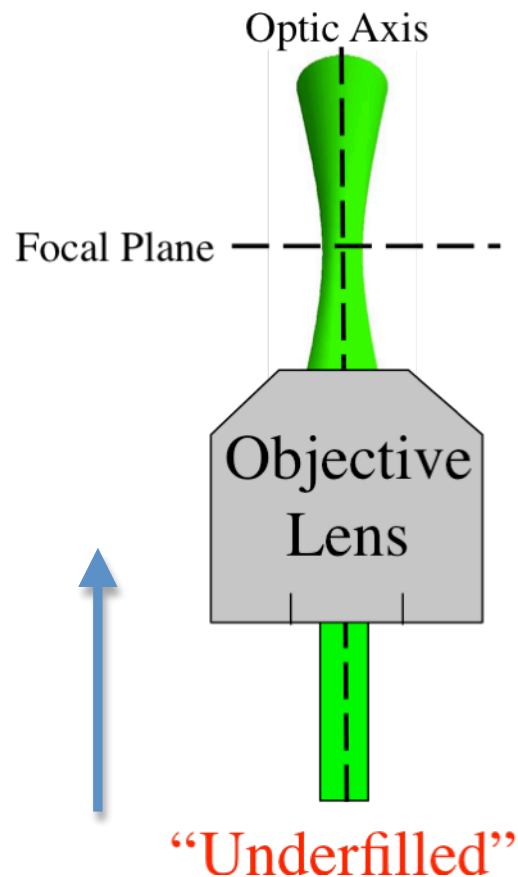
Resulting spot diameter = _____

Repeat this for your **smaller** circular aperture:

$$\begin{aligned} \text{Aperture diameter} &= \underline{\hspace{2cm}} \\ L &= \underline{\hspace{2cm}} \\ \text{Resulting spot diameter} &= \underline{\hspace{2cm}} \end{aligned}$$

Qualitatively, how does the spot size on your imaging screen scale with the diameter of the circular aperture?

This effect (diffraction) is of practical importance, as it places a limit on how well an optical device, such as a microscope or a telescope can work. Surprisingly, when light passes through a lens, a smaller **focal spot** results when a larger beam is incident upon the lens. So, to achieve the smallest spot size for high-resolution microscopy, we need a large-diameter lens, in order to accept a large-diameter beam.



High-resolution microscope objective lenses are sold according to their “**Numerical Aperture**” size, but the effective resolution depends not just upon the lens itself, but upon how it is used. – In the figure on the previous page, beam entering the objective lens is not as large as it could be; in this case, we say that the entrance pupil of the lens is “underfilled” and the result is that the focal spot is not as small as it could be.

For those interested, an interactive microscopy simulation is available online at:

<http://www.olympusmicro.com/primer/java/microscopy/airydiscs/index.html>

Surprisingly, the same effect (diffraction) that *limits* our ability to directly image small things can also put to use in ways that allow us to (indirectly) probe the structure of very small things, such as the arrangement of atoms, or molecules, in a crystal and complex molecules, such as DNA or a protein.

Part 2: Linear Apertures

In the next part of this lab, we examine this effect introducing pinhole-scale linear slits into our optical path (mostly because they are easier to “find” / align to the laser).

We will use the observed diffraction patterns that result from slits of known sizes to extract an experimental measurement of the wavelength of your laser, then turn the effect around and use your measured wavelength and the diffraction pattern that results from placing a single strand of hair in the beam to measure the width of that strand of hair very precisely. Finally, we will move on to examine the diffraction pattern of some two-dimensional structures.

If the aperture is a single linear slit, then the diffraction will produce a linear pattern with multiple maxima separated by nodes, as seen in Figure 3. The largest maximum is known as the central fringe.

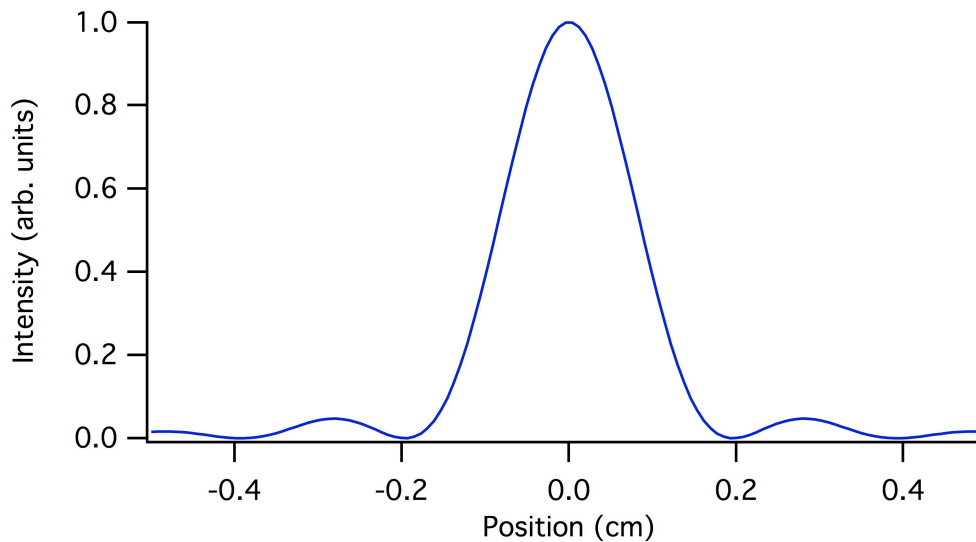


Figure 3: Single Slit Diffraction

Why?

Again, everything we are exploring this week is a consequence of the fact that light does **not** propagate in the way suggested by the simple ray diagrams used in the geometric optics approximation.

Instead, light propagates in a wave-like manner, and – for a very wide variety of wave types – we typically find that when two waves meet, the amplitudes simply add (an observation we sometimes glorify as “the superposition principle”). But what if, at the point (in space and in time) where those two waves meet, one of the waves is at minimum in its cycle while the other is at a maximum? – The result, called “destructive interference” is *still* describable as simple addition of the two wave amplitudes (with crests counting as positive amplitude and troughs counting as negative amplitude). To determine whether CONSTRUCTIVE or DESTRUCTIVE interference will occur at any particular point of measurement on our observation screen, we need to consider the effects of any time lags that might accrue along different *paths* to the same point of observation.

Keep in mind that we use sinusoidal functions to describe simple waves, and that these expect an angle as their argument (also called a “phase angle”); the *result* is that time lags can also be expressed as a shift in the overall magnitude of the argument, the phase angle.

By explicitly considering the time lags (or phase shifts) that are associated with different paths coming from different parts of the aperture, we can show that the locations of the **minima** in Figure 1 are analytically given by the Equation 1 below, and the **intensity** is described by Equation 2:

$$m\lambda = a \sin \theta \quad (1)$$

$$I = I_o \left[\frac{\sin\left(\frac{\pi a \sin \theta}{\lambda}\right)}{\frac{\pi a \sin \theta}{\lambda}} \right]^2 \quad (2)$$

where m is an integer “index” used to count which of the minima we are referring to (*e.g.*, the two minima closest to the central fringe have an index of 1, the second closest have an index of 2, and so on). Here, I_o is the intensity of the central fringe, λ is the wavelength of the light diffracted, **a is the width of the slit**, and θ is the angle (with respect to the optic axis) made by a ray emanating from the slit and traveling to the **point of measurement** on the observing screen.

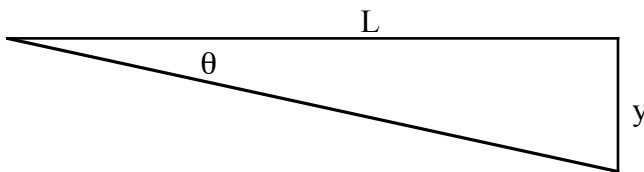


Figure 4

When the angle of diffraction, θ , is small, we can make a **small angle approximation**:

$$\sin \theta \approx \theta \approx \tan \theta = \frac{y}{L}$$

In the limit of small angles, our *predictions*, Equations (1) and (2), become:

$$m\lambda = a \frac{y}{L} \quad (3)$$

$$I = I_0 \left[\frac{\sin\left(\frac{\pi ay}{\lambda L}\right)}{\frac{\pi ay}{\lambda L}} \right]^2 \quad (4)$$

Place the slide with a **single slit** aperture (Slide 9165-A) in the location labeled “Slit” in Figure 1. Adjust its position to optimize the brightness of the resulting diffraction pattern. **Sketch** the observed diffraction pattern.

From fitting your observations to the predictions above, you can extract an experimental measurement of your laser’s wavelength:

Width of slit = _____
 $L \pm dL =$ _____

m	$y \pm dy$	$\lambda_{\text{experimental}}$	% error
1			
2			
3			

Which order provides the more *precise* measure of the laser’s wavelength, $m = 1$ or $m = 3$? Why?

Repeat this experiment with another single slit aperture from Slide 9165-A:

Width of slit = _____
 $L \pm dL =$ _____

m	$y \pm dy$	$\lambda_{\text{experimental}}$	% error
1			
2			
3			

Which slit provides the more *accurate* measure of the laser’s wavelength, the larger slit or the smaller one?

Part 3: A single strand of hair

In the next part of this lab, use your measured wavelength from part 2 and the diffraction pattern that results from placing a single strand of hair in the beam (instead of the slit) to measure the width of that strand of hair very precisely. – If the strand of hair is oriented along the same direction that your slit aperture was, then all you’ve done by changing from the slit to the hair is to swap what was opaque in the diffracting plane with what was transparent. On the basis of this *symmetry* you can expect that the resulting pattern on your observing screen will be much like the pattern observed in Part 2, but with a reversal of dark and bright areas.

$$\lambda \pm d\lambda = \underline{\hspace{2cm}}$$
$$L \pm dL = \underline{\hspace{2cm}}$$

m	y
1	
2	
3	

What should you report as your experimental result for the diameter of the hair?

If you used a thinner strand of hair, how would that change the spacings between minima in the diffraction pattern?

Part 4: Diffractive Optics

Once you realize that the output of a laser beam can be “sculpted” by any *time lags* introduced into the beam path, an easy opportunity for creative expression is unleashed. – Because the **index of refraction** of plastic is different from that of air, simply stamping a texture into plastic will introduce phase shifts of one part of the beam relative to another. At each station there is a plastic sheet from “Digital Optics Corporation” containing a variety of textures for you to inspect.

Step A: So that the laser beam is large enough to sample the full texture stamped on each square of the plastic sheet, you first need to construct a “**beam expander**” by using two lenses (18mm and 252mm, with the **smaller focal length positioned closer to the laser**), separated by the sum of their focal lengths. TEST that the output is “collimated” by using an index card: if the separation between lenses is too much, then the beam will shrink as you move the card further away; if the separation is too little, then the beam will expand.

Step B: Using your expanded your laser beam, inspect the output generated by at least three squares on the plastic sheet (“keyboard,” “eye,” and “bride”)

Given what you've observed so far, it may not surprise you to learn that the patterns stamped into the plastic **look *nothing* like** the desired output intensity patterns! After all, you now know that if you want to generate a small spot, you need a big region on the input, ... and that if you want to generate a large spot, you need a very small region on the input. *Everything* in the customized textures stamped into the plastic sheets had to be designed in this *topsy-turvy* way:

There is a *reciprocal* relationship between the texture in the diffractive optic and the resulting intensity pattern created far away.

Questions

1. In this experiment, we used a helium-neon laser, with $\lambda = 632.8$ nm. How narrow should your slit be, if you only want the first maxima to fit on the screen or sheet of paper you used for viewing the pattern?

2. Would a violet laser, $\lambda = 400$ nm, improve the accuracy of the measurement that you made on the wavelength? Why or why not?

Initiative

Conclusions